
Chapter 2

graph formating

```
In[1]:= thinn = AbsoluteThickness[.5];  
medum = AbsoluteThickness[1.];  
thick = AbsoluteThickness[1.5];  
black = GrayLevel[0];  
BGray = GrayLevel[0.3];  
WGray = GrayLevel[0.6];  
SetOptions[Plot, PlotStyle -> {{thinn, Black}, {thinn, Black}, {thinn, Black}},  
PlotPoints -> 40, ImageSize -> 360,  
FrameStyle -> medum, AxesStyle -> medum,  
BaseStyle -> {FontFamily -> "Helvetica", FontSlant -> Plain, FontSize -> 12}];  
SetOptions[ListPlot, AxesStyle -> medum, PlotStyle -> medum, ImageSize -> 384,  
BaseStyle -> {FontFamily -> "Helvetica", FontSlant -> "Plain", FontSize -> 12}];  
SetOptions[ParametricPlot, PlotStyle ->  
{{thinn, Black}, {thinn, Black}, {thinn, Black}}, PlotPoints -> 40,  
FrameStyle -> medum, AxesStyle -> medum, PlotStyle -> medum,  
BaseStyle -> {FontFamily -> "Helvetica", FontSlant -> "Plain", FontSize -> 12}];  
SetOptions[Graphics, BaseStyle ->  
{FontFamily -> "Helvetica", FontSlant -> "Plain", FontSize -> 12}];
```

2.8 Detour; Benefit Calculations

Linear

```
In[11]:= p = .;  
w = .;  
q0 = 35 000.;  
p0 = 3.;  
elast = -0.5;  
m = elast * q0 / p0;  
b = q0 - m * p0;  
wlin = m * p + b  
plin = p /. Flatten[Simplify[Solve[w == %, p]]]
```

```
Out[18]= 52 500. - 5833.33 p
```

```
Out[19]= 9. - 0.000171429 w
```

LogLinear

```
In[20]:= c = q0 / p0^elast;
wlog = c * p^elast
plog = p /. Flatten[Simplify[Solve[w == %, p]]]
```

```
Out[21]= 
$$\frac{60\,621.8}{p^{0.5}}$$

```

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

```
Out[22]= 
$$\frac{3.675 \times 10^9}{w^{2.0000000000000000}}$$

```

2.9 MNB

```
In[23]:= mc = 1.95 + 0.00003 * w;
mnblog = plog - mc
```

```
Out[24]= 
$$-1.95 + \frac{3.675 \times 10^9}{w^{2.0000000000000000}} - 0.00003 w$$

```

2.10, 2.11 Two MNBs

```
In[25]:= plog2 = plog * 0.5;
mc2 = 1.5 + 0.00002 * w;
mnblog2 = plog2 - mc2;
flipmnblog2 = mnblog2 /. w -> (50 000 - w);
FindRoot[mnblog - flipmnblog2 == 0, {w, 25 000}]
mnblog /. %
```

```
Out[29]= {w -> 28 056.2}
```

```
Out[30]= 1.87707
```

2.12 Two Sectors with One Yielding Return Flow

Method I - graphed

```
In[31]:= R = 0.25;
flipmnblog2R = mnblog2 /. w -> (50 000 - (1 - R) * w)
```

```
Out[32]= 
$$-1.5 + \frac{1.8375 \times 10^9}{(50\,000 - 0.75 w)^{2.0000000000000000}} - 0.00002 (50\,000 - 0.75 w)$$

```

```
In[33]:= FindRoot[mnblog / (1 - R) - flipmnblog2R == 0, {w, 25 000}]
mnblog /. %
```

```
Out[33]= {w -> 32 407.3}
```

```
Out[34]= 0.576995
```

Method 2

```
In[35]:= mnb1 = mnblog / . w → w1  
mnb2 = mnblog2 / . w → w2
```

$$\text{Out[35]= } -1.95 + \frac{3.675 \times 10^9}{w_1^{2.0000000000000000}} - 0.00003 w_1$$

$$\text{Out[36]= } -1.5 + \frac{1.8375 \times 10^9}{w_2^{2.0000000000000000}} - 0.00002 w_2$$

```
In[37]:= FindRoot[{mnb1 == (1 - R) * mnb2, (1. - R) * w1 + w2 == 50 000}, {w1, 25 000}, {w2, 25 000}]
```

```
Out[37]= {w1 → 32 407.3, w2 → 25 694.5}
```

```
In[38]:= {mnb1, mnb2} /. %
```

```
Out[38]= {0.576995, 0.769327}
```

2.13 MNB Addition for Nonrival Uses (vs Rival)

Assuming the a,b line has a lower p intercept ($a < c$) and a higher q intercept ($a/b > c/d$):

```

In[39]:= Clear[a, b, c, d]
d1 = a - b * q;
d2 = c - d * q;
q1 = a / b - p / b;
q2 = c / d - p / d;
Solve[qp == q1 + q2, p]
{a, b, c, d} = {6., 1, 10., 3.};
nonrivalgd = Which[0 <= q <= c / d, a + c - (b + d) q,
  c / d < q <= a / b, d1,
  a / b < q, 0];
rivalgd = Which[0 <= q <= (c - a) / d, d2,
  (c - a) / d < q <= c / d + a / b,
  (b * c + a * d - b * d * q) / (b + d)];

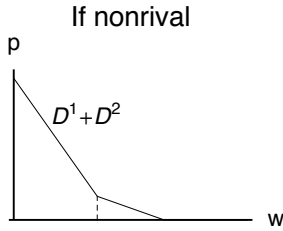
pl213i = Plot[{d1, d2}, {q, 0, c / d + a / b},
  PlotRange -> {0, a + c + 1}, AxesOrigin -> {0, 0},
  AxesLabel -> {"w", "p"}, Ticks -> None, PlotLabel -> "Two demands"];
pl213ii = Show[pl213i,
  Graphics[Text["D1", {1.3, 9}]],
  Graphics[Text["D2", {5, 3}]], Graphics[{Dashing[ {.02, .02}], thinn,
  Line[{{c / d, 0.}, {c / d, a + c}], Line[{{0., a}, {c / d + a / b, a}]}]}];
pl213iii = Plot[nonrivalgd, {q, 0, c / d + a / b},
  PlotRange -> {0, a + c + 1}, AxesOrigin -> {0, 0},
  AxesLabel -> {"w", "p"}, Ticks -> None, PlotLabel -> "If nonrival"];
pl213iv = Show[pl213iii,
  Graphics[Text["D1+D2", {2.9, 12}]], Graphics[
  {Dashing[ {.02, .02}], thinn, Line[{{c / d, 0.}, {c / d, a - b * c / d}]}]}];
pl213v = Plot[rivalgd, {q, 0, c / d + a / b},
  PlotRange -> {0, a + c + 1}, AxesOrigin -> {0, 0},
  AxesLabel -> {"w", "p"}, Ticks -> None, PlotLabel -> "If rival"];
pl213vi = Show[pl213v,
  Graphics[Text["D1+D2", {5, 6}]],
  Graphics[{Dashing[ {.02, .02}], thinn, Line[{{0., a}, {(c - a) / d, a}]}]}];
pl213 = Show[GraphicsGrid[{{pl213iv, Null},
  {pl213ii, pl213vi}}], ImageSize -> 400]

```

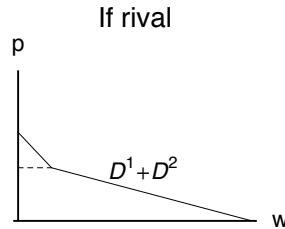
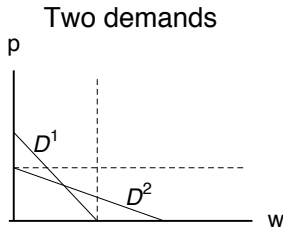
```

Out[44]= {{p ->  $\frac{bc + ad - bdqp}{b + d}$ }}

```



Out[54]=

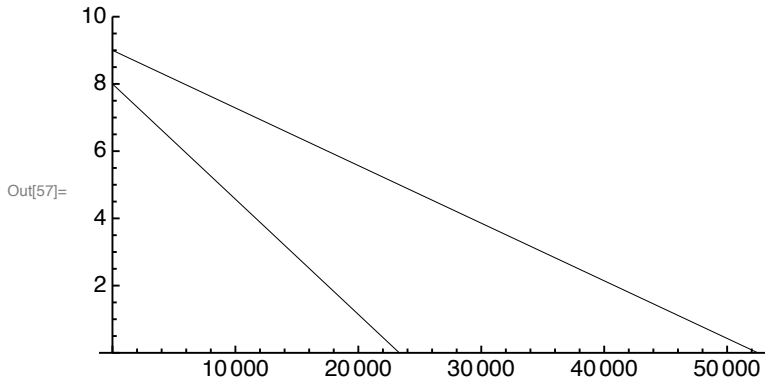


2.14-2.16 Neutral Efficiency

```
In[55]:= plin
plin2 = Expand[plin * 2. - 10.]
Plot[{plin, plin2}, {w, 0, 52500},
PlotRange -> {0, 10},
AspectRatio -> 0.5]
```

Out[55]= 9. - 0.000171429 w

Out[56]= 8. - 0.000342857 w



Assuming the a,b line has a lower p intercept ($a < c$) and a higher q intercept ($a/b > c/d$):

```
In[58]:= Clear[a, b, c, d]
d1 = a - b * q;
d2 = c - d * q;
q1 = a / b - p / b;
q2 = c / d - p / d;
Solve[q * p == q1 + q2, p]
```

Out[63]= $\left\{ \left\{ p \rightarrow \frac{bc + ad}{b + d + bdq} \right\} \right\}$

```
In[64]:= {a,b,c,d}={8.,0.000342857,9.,0.000171429};
dtotal=Which[0<=q<=(c-a)/d,d2,
             (c-a)/d<q<=c/d+a/b,
             (b*c+a*d-b*d*q)/(b+d)]
```

```
Out[65]= Which[0 ≤ q ≤ 5833.32, d2,  $\frac{c-a}{d} < q \leq \frac{c}{d} + \frac{a}{b}, \frac{bc+ad-bdq}{b+d}$ ]
```

```
In[66]:= v = p /. Flatten[Solve[((b*c+a*d-b*d*55000)/(b+d)) == p, p]]
```

```
Out[66]= 2.38094
```

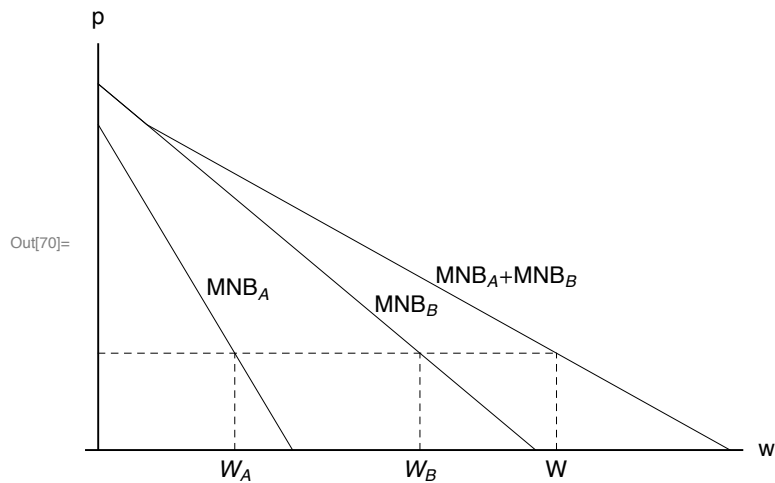
```
In[67]:= wa = q1 /. p → v
         wb = q2 /. p → v
```

```
Out[67]= 16388.9
```

```
Out[68]= 38611.1
```

```
In[69]:= pl214i = Plot[{d1, d2, dtotal}, {q, 0, c/d+a/b},
                    PlotRange → {0, c+1}, AxesOrigin → {0, 0}, AxesLabel → {"w", "p"},
                    Ticks → {{{wa, "WA", 0}, {wb, "WB", 0}, {55000, "W", 0}}, {{v, "", 0}}];
```

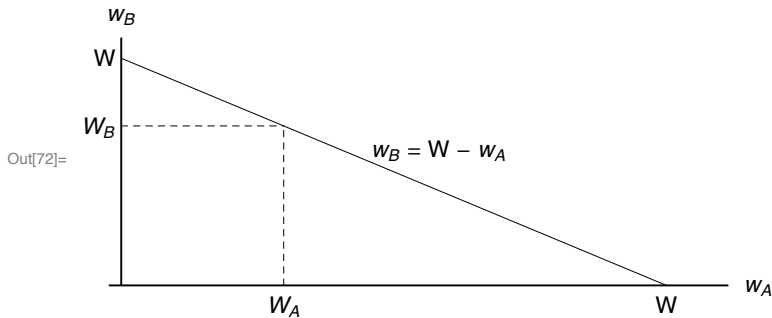
```
In[70]:= pl214 = Show[pl214i,
                    Graphics[Text["MNBA", {16800, 4}]],
                    Graphics[Text["MNBB", {37000, 3.6}]],
                    Graphics[Text["MNBA+MNBB", {49000, 4.3}]],
                    Graphics[{Dashing[ {.01, .01}], thinn,
                               Line[{{55000, 0}, {55000, v}}],
                               Line[{{0, v}, {55000, v}}],
                               Line[{{wa, 0}, {wa, v}}],
                               Line[{{wb, 0}, {wb, v}}]}]]]
```



```

In[71]:= pl215a = Plot[55 000 - wa, {wa, 0, 60 000},
  PlotRange -> {0, 60 000},
  AxesOrigin -> {0, 0},
  AspectRatio -> 0.9,
  AxesLabel -> {"w_A", "w_B"},
  Ticks -> {{{wa, "w_A", 0}, {55 000, "W", 0}}, {{wb, "w_B", 0}, {55 000, "W", 0}}},
  DisplayFunction -> Identity];
pl215 = Show[pl215a,
  Graphics[Text["w_B = W - w_A", {32 000, 33 000}]],
  Graphics[{Dashing[ {.01, .01}], thinn,
    Line[{{wa, 0}, {wa, wb}}],
    Line[{{0, wb}, {wa, wb}}]}],
  ImageSize -> 360,
  AspectRatio -> 0.4]

```



```

In[73]:= NBA = ∫₀ᵂ d1 dq
NBB = ∫₀ᵂ d2 dq

```

Out[73]= 8. w - 0.000171429 w²

Out[74]= 9. w - 0.0000857145 w²

```

In[75]:= sata = q /. Flatten[Solve[d1 == 0, q]]
satb = q /. Flatten[Solve[d2 == 0, q]]

```

Out[75]= 23 333.3

Out[76]= 52 499.9

So the Pareto frontier should only be plotted so the neither sector gets more than their satiation amounts (a's is 23333, b's is 52500).

```

In[77]:= NBA /. w -> wa
NBA /. w -> sata
NBB /. w -> wb
NBB /. w -> satb

```

Out[77]= 85 066.2

Out[78]= 93 333.4

Out[79]= 219 715.

Out[80]= 236 249.

```
In[81]:= effpt = {85 066.2, 219 715.}
```

```
Out[81]= {85 066.2, 219 715.}
```

```
In[82]:= flipNBB = NBB /. w → (55 000 - w)
```

```
Out[82]= 9. (55 000 - w) - 0.0000857145 (55 000 - w)2
```

```
In[83]:= pl216i = ParametricPlot[{NBA, flipNBB}, {w, 55 000 - satb, sata},
  PlotStyle → {{thinn, Black}},
  AxesLabel → {"NBA", "NBB"},
  AxesOrigin → {0, 150 000},
  AspectRatio → .5,
  PlotRange → {{0, 108 000}, {150 000, 250 000}}];
pl216 = Show[pl216i, Graphics[{PointSize[.015], Point[effpt]}],
  ImageSize → 360,
  AspectRatio → 0.5]
```

