
redoing the "Drawing from a Reservoir" model

dynamic parameters

```
In[1]:= T = 2;  
d = .06;  
g = .01;
```

benefits (build demand using parameters from Chap 2 and integrate under it)

```
In[4]:= q0 = 35 000;  
p0 = 3;  
elast = -1 / 2;  
c = q0 / p0^elast;  
wlog = (1 + g) ^ (t - 1) * c * p^elast;  
mb = p /. Flatten[Simplify[Solve[w == %, p]]];
```

```
In[10]:= Assuming [ {W > 100}, tb =  $\int_{100}^W mb \, dw$  ]
```

```
Out[10]= 
$$\frac{3.60259 \times 10^7 e^{0.0199007 t} (-100. + W)}{W}$$

```

costs

```
In[11]:= tc = 50 000 + 1.95 * W + 0.000015 * W^2;
```

hydrologics

Numbers in line 1 of following cell are opt water uses for 1st 2 periods as computed in chap 3. The intent here is to compute a reservoir amount which exactly allows this 2-period consumption assuming mean inflows of 27000.

```
In[12]:= initialstored = 31 573.3 + 31 673.4 - 2 * 27 000  
annualflow = 27 000;
```

```
Out[12]= 9246.7
```

develop work matrix

```
In[14]:= wvector = Prepend[Array[w, T - 1], w0];
work = Table[1., {t, T}, {j, 8}];
work[[1, 1]] = 0;
Do[work[[t + 1, 1]] = t, {t, T - 1}]
Do[work[[t, 2]] = W /. Flatten[Solve[D[(tb - tc), W] == 0, W, Reals]], {t, 1, T}]
Do[work[[t, 3]] = wvector[[t]], {t, T}]
Do[work[[t, 4]] = (tb - tc) /. W → work[[t, 3]], {t, T}]
Do[work[[t, 5]] = work[[t, 4]] / (1 + d)^(t - 1), {t, T}]
work[[1, 6]] = initialstored + annualflow;
Do[work[[t, 6]] = work[[t - 1, 6]] + annualflow - work[[t - 1, 3]], {t, 2, T}]
work[[1, 7]] = initialstored + annualflow;
work[[1, 8]] = Min[work[[1, 2]], work[[1, 7]]];
Do[{work[[t, 7]] = work[[t - 1, 7]] + annualflow - work[[t - 1, 8]],
  work[[t, 8]] = Min[work[[t, 2]], work[[t, 7]]]}, {t, 2, T}]
rslts = TableForm[Prepend[work, {"Period", "MNB=0@", "w", "NBs",
  "PV(NBs)", "Reserv@Start", "MyopicReserv", "MyopicUse"}]];
Dual = D[work[[1, 4]], w0];
```

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Expected NPV

A crude bit of re-coding and amenable to only two periods as written here. Run separately for each line of Table 4.1.

```
In[36]:= w0 = .;
centerprob = 1 / 3.;
overunder = 8000.;
enpv = Simplify[work[[1, 5]]
+ (((1. - centerprob) / 2.) * (work[[2, 5]] /.
  w[1] → (-w0 + initialstored + annualflow + annualflow - overunder)))
+ (centerprob * (work[[2, 5]] /. w[1] → (-w0 + initialstored +
  annualflow + annualflow)))
+ (((1. - centerprob) / 2.) * (work[[2, 5]] /. w[1] →
  (-w0 + initialstored + annualflow + annualflow + overunder)))]];
answr = NMaximize[{enpv, w0 ≥ 0.}, w0];
w0 = w0 /. Flatten[answr[[2]]]
Dual
```

Out[41]= 30 704.3

Out[42]= 1.02702